

# **Dynamics of Multi-Phase Interstellar Medium with and without Magnetic Field**

**Shu-ichiro Inutsuka (Kyoto Univ.)**

Collaboration with

**Hiroshi Koyama** (Univ. Maryland)

**Tsuyoshi Inoue** (Kyoto Univ.)

**Patrick Hennebelle** (Paris Obs. & ENS)

**Masahiro Nagashima** (Nagasaki Univ.)

**Keywords:**

radiative cooling/heating, thermal instability,  
MHD, supersonic velocity dispersion, etc.

# "Turbulence" in Molecular Clouds

Linewidth-Size Relation  
(Larson's Law)

$$\delta v \propto L^{0.5}$$

$$10^{21} \text{ cm}^{-2} \cdot N_{\text{H}_2} \cdot 10^{23} \text{ cm}^{-2}$$

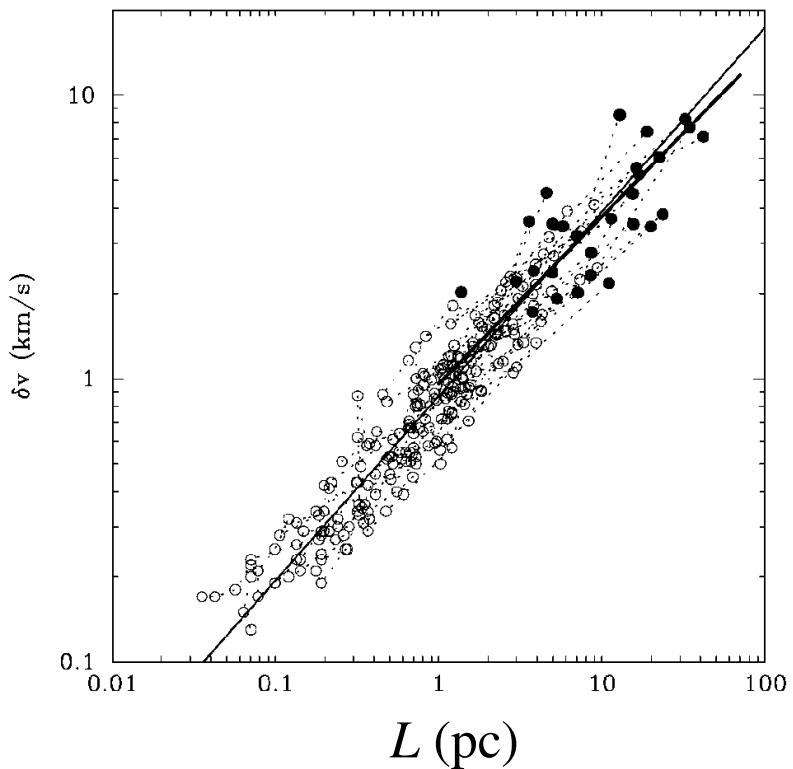


FIG. 1.—Composite  $\delta v, l$  relationship from PCA decompositions of  $^{12}\text{CO}$   $J = 1-0$  imaging observations of 27 individual molecular clouds. The small scatter of points attests to the near invariance of interstellar turbulence within molecular clouds that exhibit a large range in size, environment, and star formation activity. The large filled circles are the global velocity dispersion and size for each cloud derived from the first principal component. These are equivalent to the global velocity dispersion and size of the cloud as would be measured in the cloud-to-cloud size/line width relationship (Larson 1981; Solomon et al. 1987). The light solid line shows the bisector fit to all points from all clouds. The heavy solid line shows the bisector fit to the filled circles exclusively. The similarity of these two power laws explains the connection of Larson's cloud-to-cloud scaling law to the structure functions of individual clouds.

Heyer & Brunt 2004

# Observed “Turbulence” in ISM

## Observation of Molecular Clouds

line-width  $\delta v > C_s$

### Universal Supersonic Velocity Dispersion

even in the clouds without star formation activity

→ should not be due to star formation activity

## Numerical Simulation of (Isothermal) MHD

Turbulence  $\Rightarrow$  Rapid Shock Dissipation or Cascade

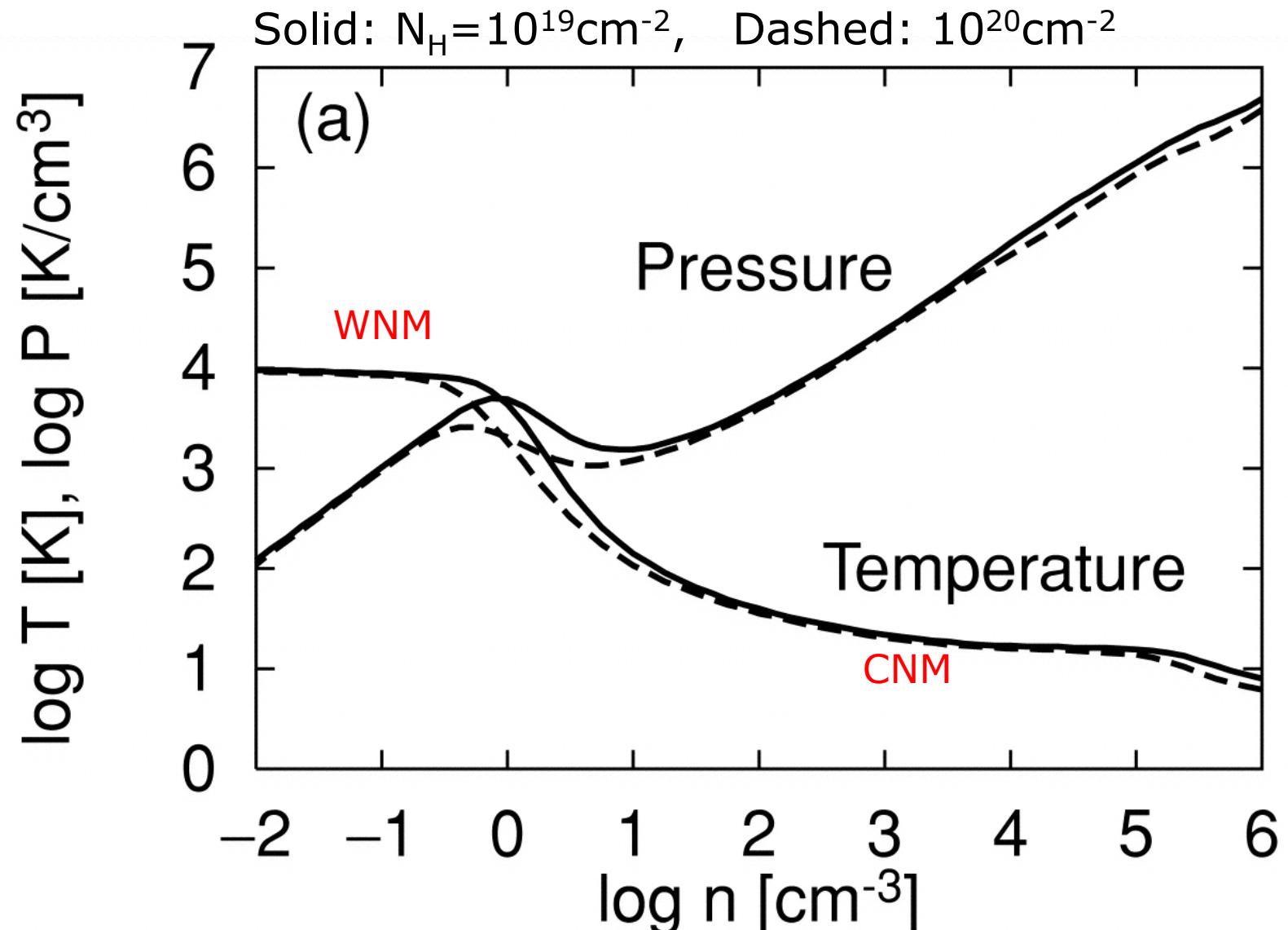
– Dissipation time « Lifetime of Molecular Clouds

- Gammie & Ostriker 1996, Mac Low 1997, Ostriker et al. 1999, Stone et al. 1999, etc...

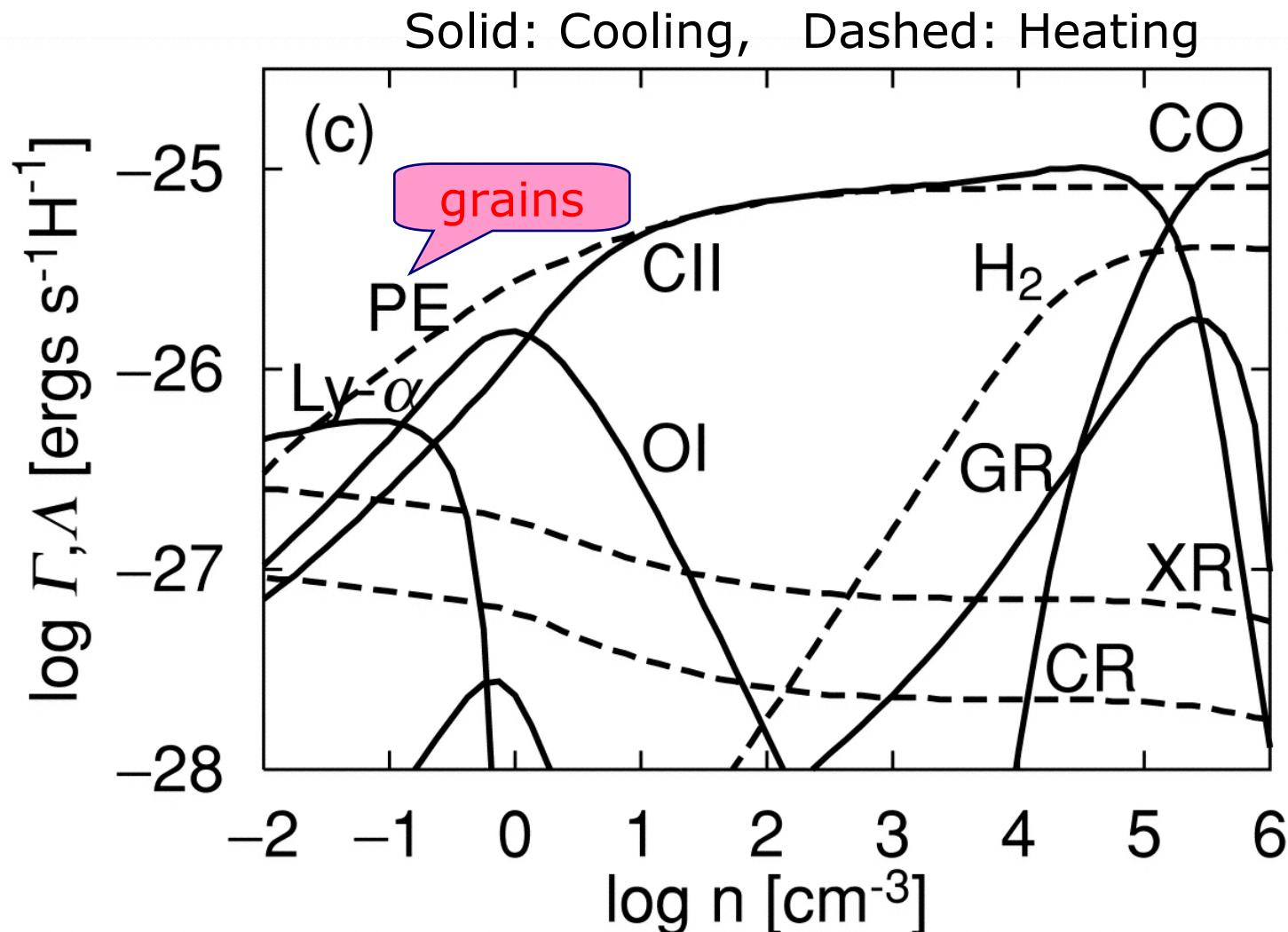
## Recent Studies on Origin of Supersonic Motions

- Koyama & Inutsuka, ApJL **564**, L97 , 2002
- Kritsuk & Norman 2002a, ApJ **569**, L127; 2002b ApJ **580**, L51
- Audit & Hennebelle 2005, A&A **433**, 1
- Heitsch, Burkert, Hartmann et al. 2005, ApJ **633**, L113, Vazquez-Semadeni et al. 2006, etc...

# Radiative Equilibrium



# Radiative Cooling & Heating



Koyama & Inutsuka (2000) ApJ 532, 980 , based on Wolfire et al. 1995

# Basic Equations

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho v) = 0,$$

$$\frac{\partial v}{\partial t} + v \cdot \nabla v = -\frac{1}{\rho} \nabla P + \frac{(\nabla \times B) \times B}{4\pi\rho},$$

$$\frac{\partial \rho e}{\partial t} + \nabla \cdot (\rho e v) + P \nabla \cdot v - \frac{|(\nabla \times B) \times B|^2}{16\pi^2 A \rho \rho_i} = \rho \Gamma - \rho^2 \Lambda(T) + \nabla \cdot (K \nabla T),$$

$$\frac{\partial B}{\partial t} = \nabla \times (v_i \times B),$$

radiative heating/cooling

$$v_i - v = \frac{(\nabla \times B) \times B}{4\pi A \rho \rho_i},$$

thermal conduction

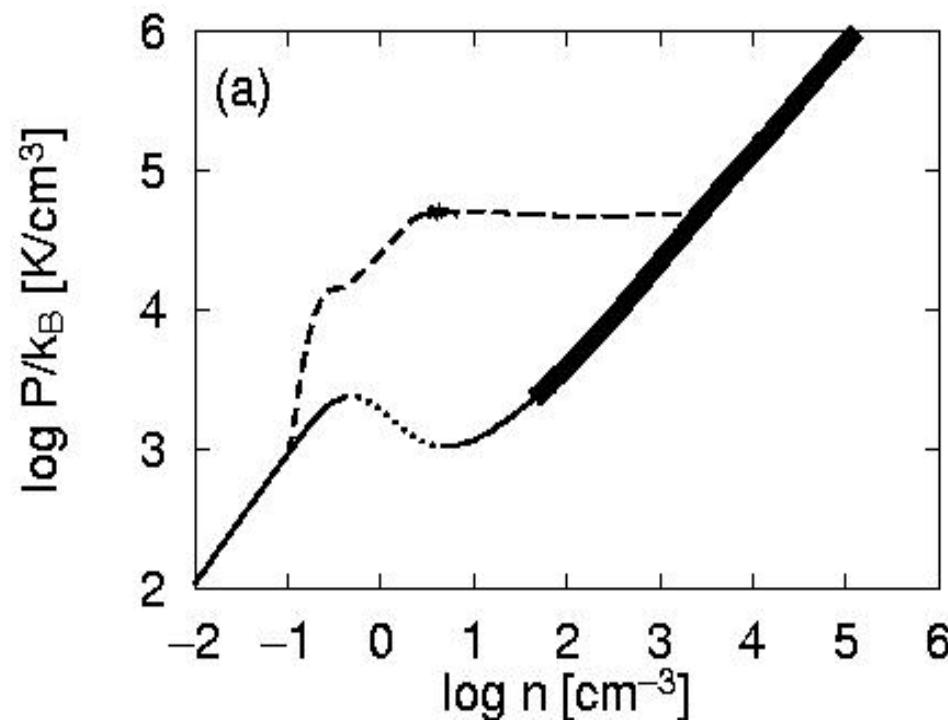
$$\rho_i = m_H n(HII) + 12m_H n f_{CII},$$

$$0 = \zeta n(HI) - n(HII) n(e) \alpha(T),$$

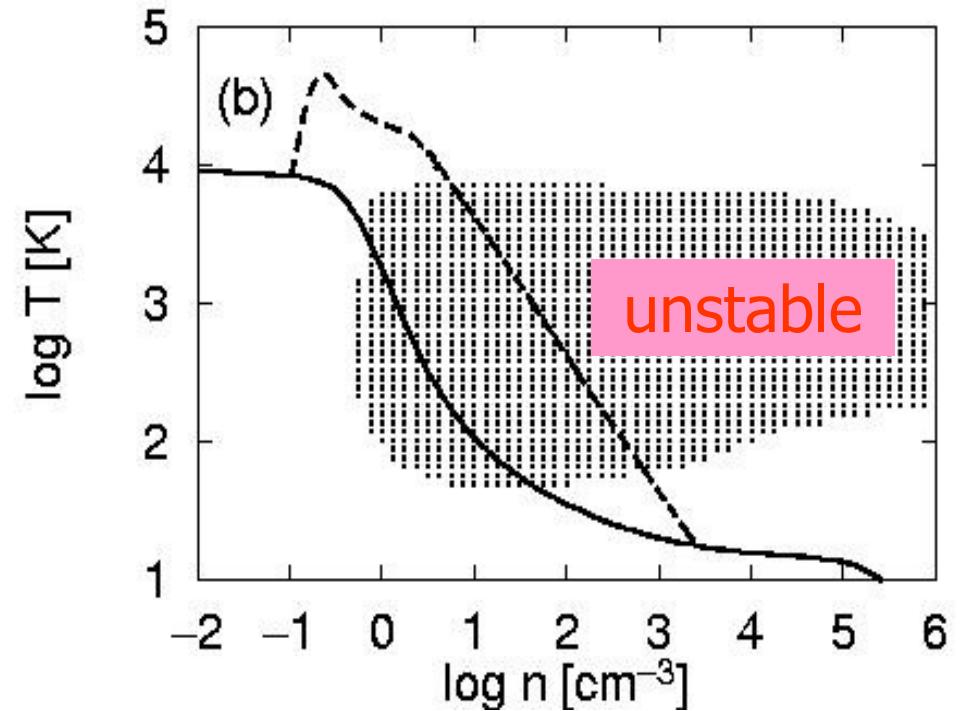
$$n(e) = n(HII) + n f_{CII}.$$

# 1D Shock Propagation into WNM

Density-Pressure Diagram



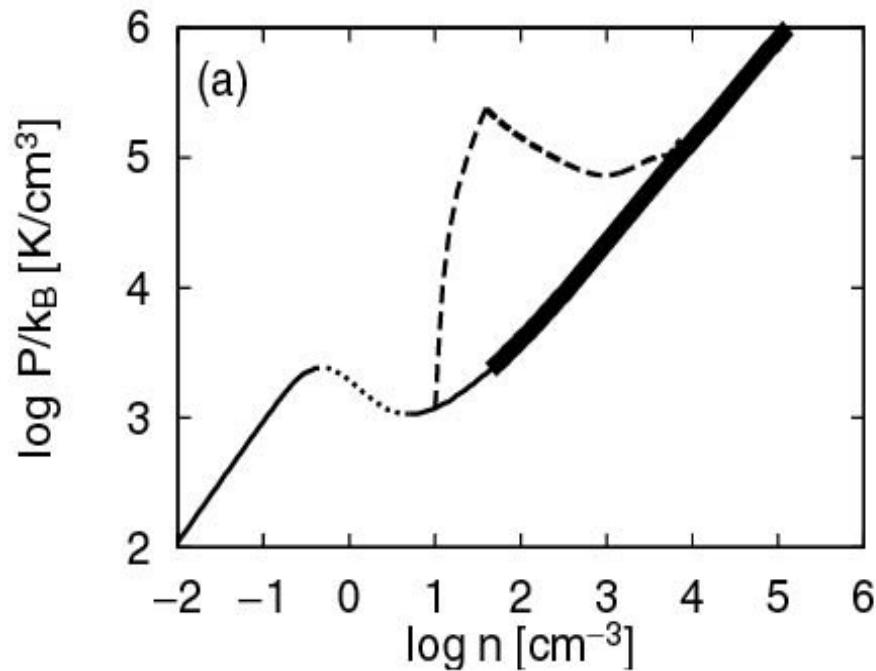
Density-Temperature Diagram  
– through unstable region



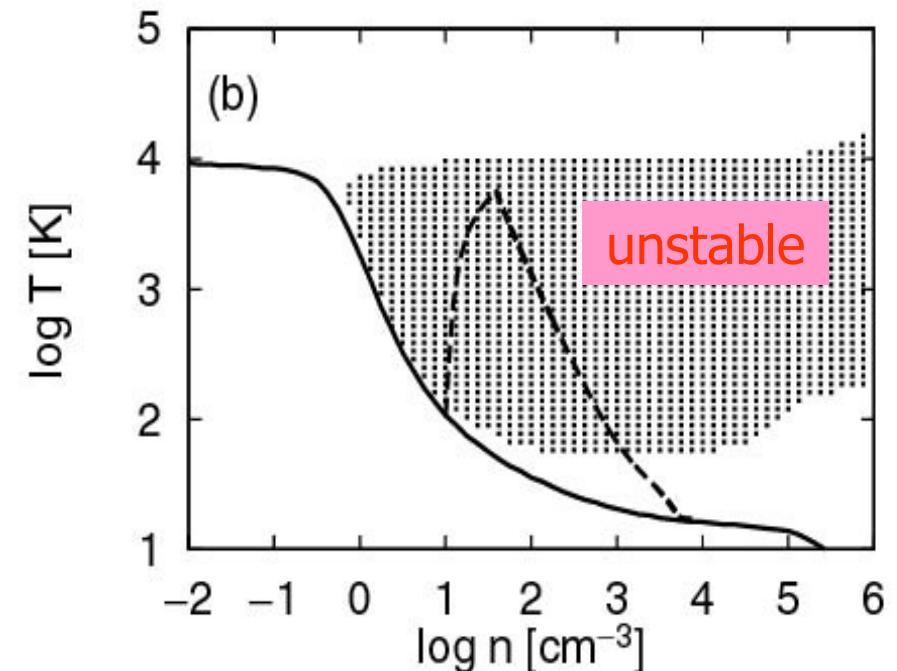
Koyama & Inutsuka 2000, ApJ **532**, 980  
See also Hennebelle & Pérault 1999

# 1D Shock Propagation into CNM

Density-Pressure Diagram



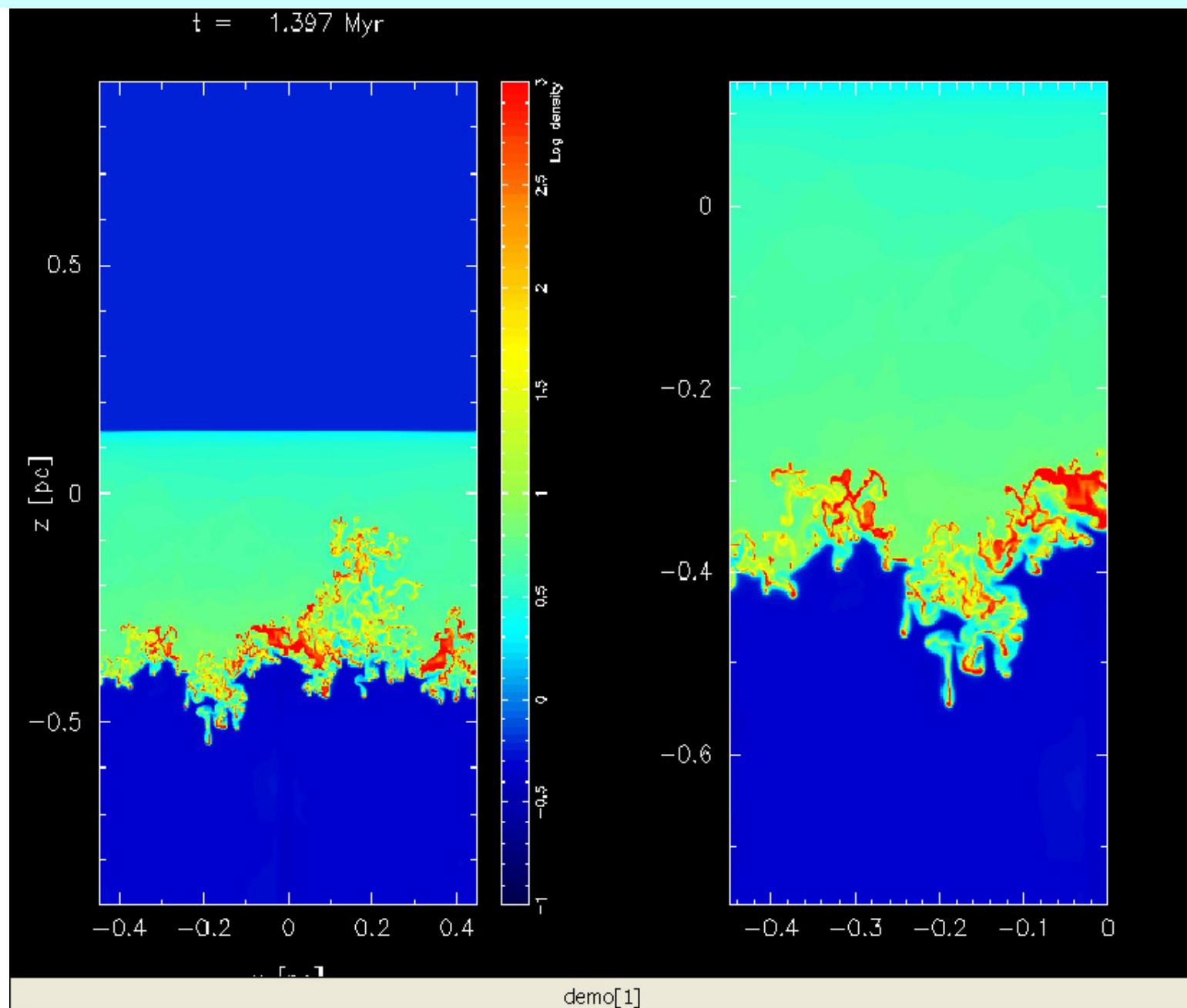
Density-Temperature Diagram



CNM becomes thermally unstable with shock.

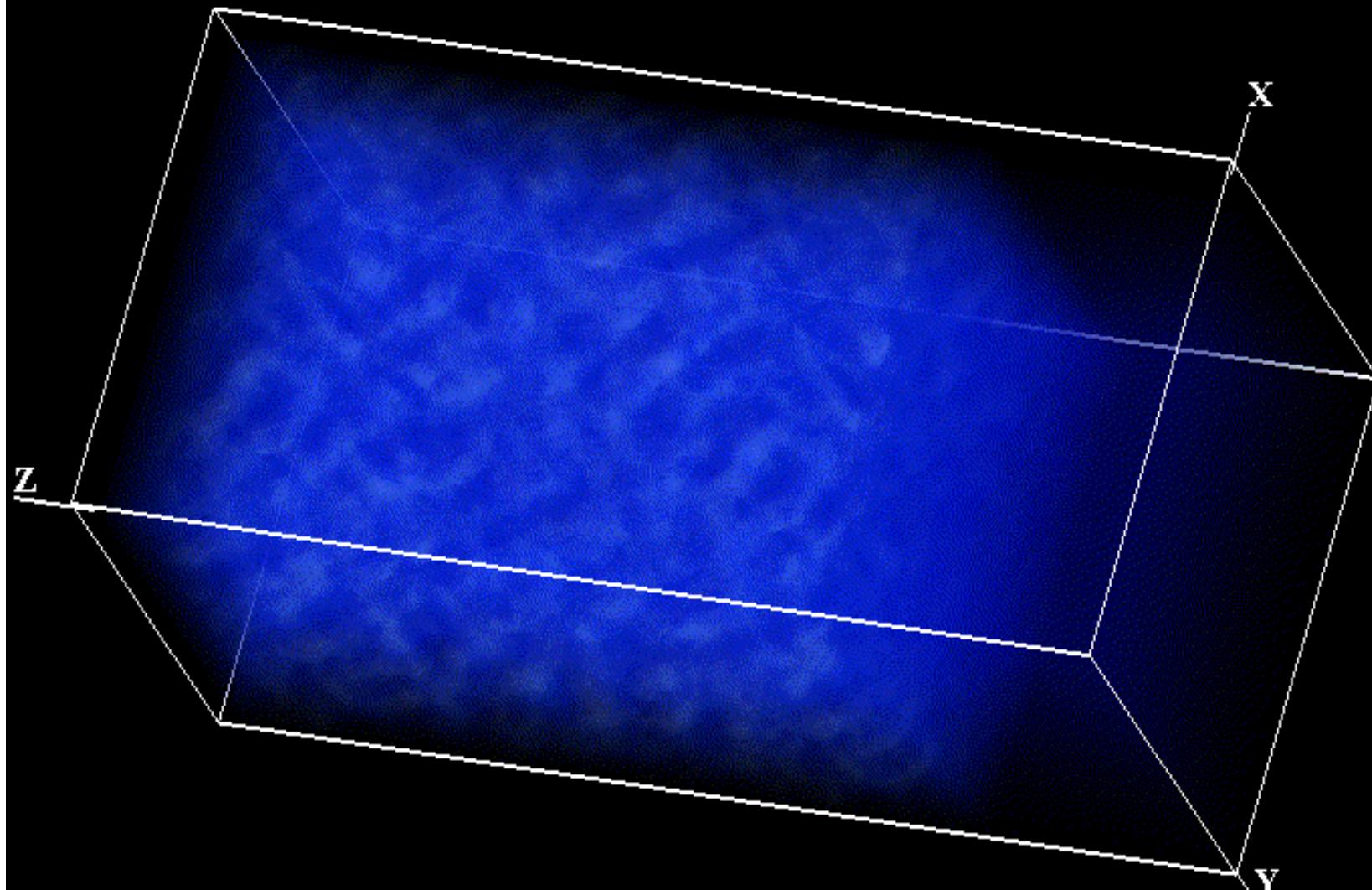
Koyama & Inutsuka 2000, ApJ **532**, 980

# Shock Propagation into WNM

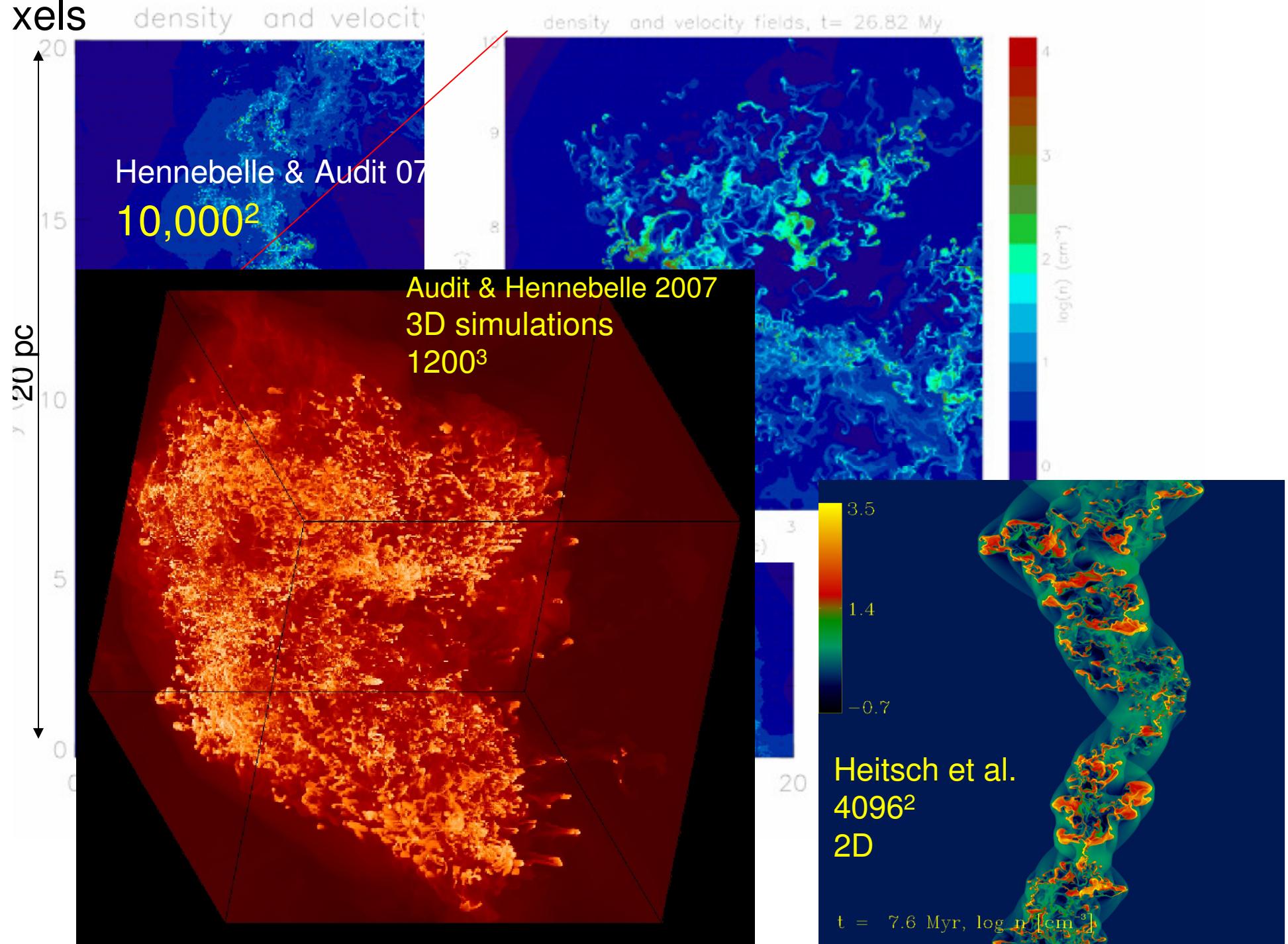


# WNM Swept-Up by 14.4km/s Shock (3D)

Koyama & Inutsuka 2002



xels



# Summary of TI-driven Turbulence

- 2D/3D Calculation of The Propagation of Shock Wave into WNM
  - via Thermal Instability
  - fragmentation of the cold layer into cold clumps with long-sustained supersonic velocity dispersion ( $\sim$  km/s)

1D:      Shock  $\Rightarrow E_{\text{th}} \Rightarrow E_{\text{rad}}$

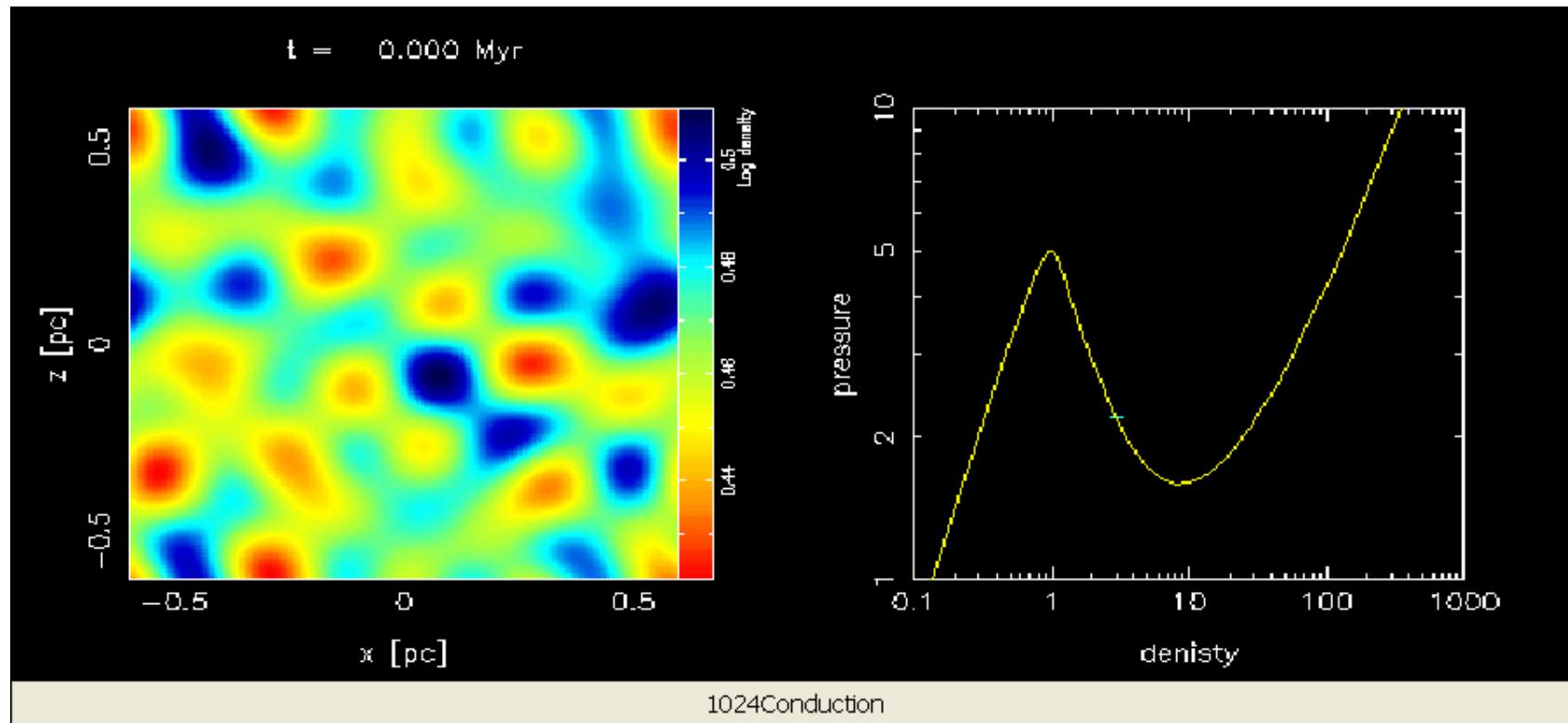
2D&3D: Shock  $\Rightarrow E_{\text{th}} \Rightarrow E_{\text{rad}} + E_{\text{kin}}$

$$\delta v \sim \text{a few km/s} < C_{S,\text{WNM}}$$

## Further Analysis

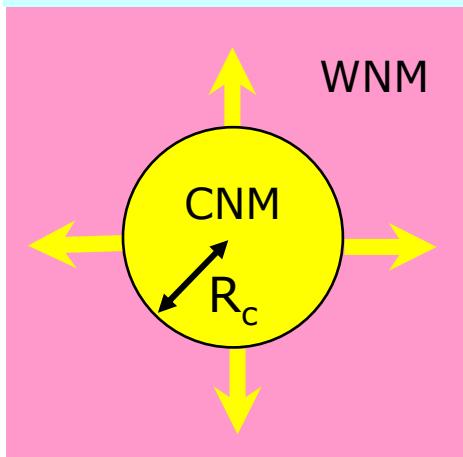
- Driving Mechanism
- Evaporation & Condensation
- Instability of Transition Layer
- Effect of Magnetic Field

# 2D Evolution from Unstable Equilibrium



Periodic Box Evolution without Shock Driving  
With Cooling/Heating and Thermal Conduction  
Without Physical Viscosity  $\rightarrow \text{Pr} = 0$

# Evaporation of Spherical CNM in WNM

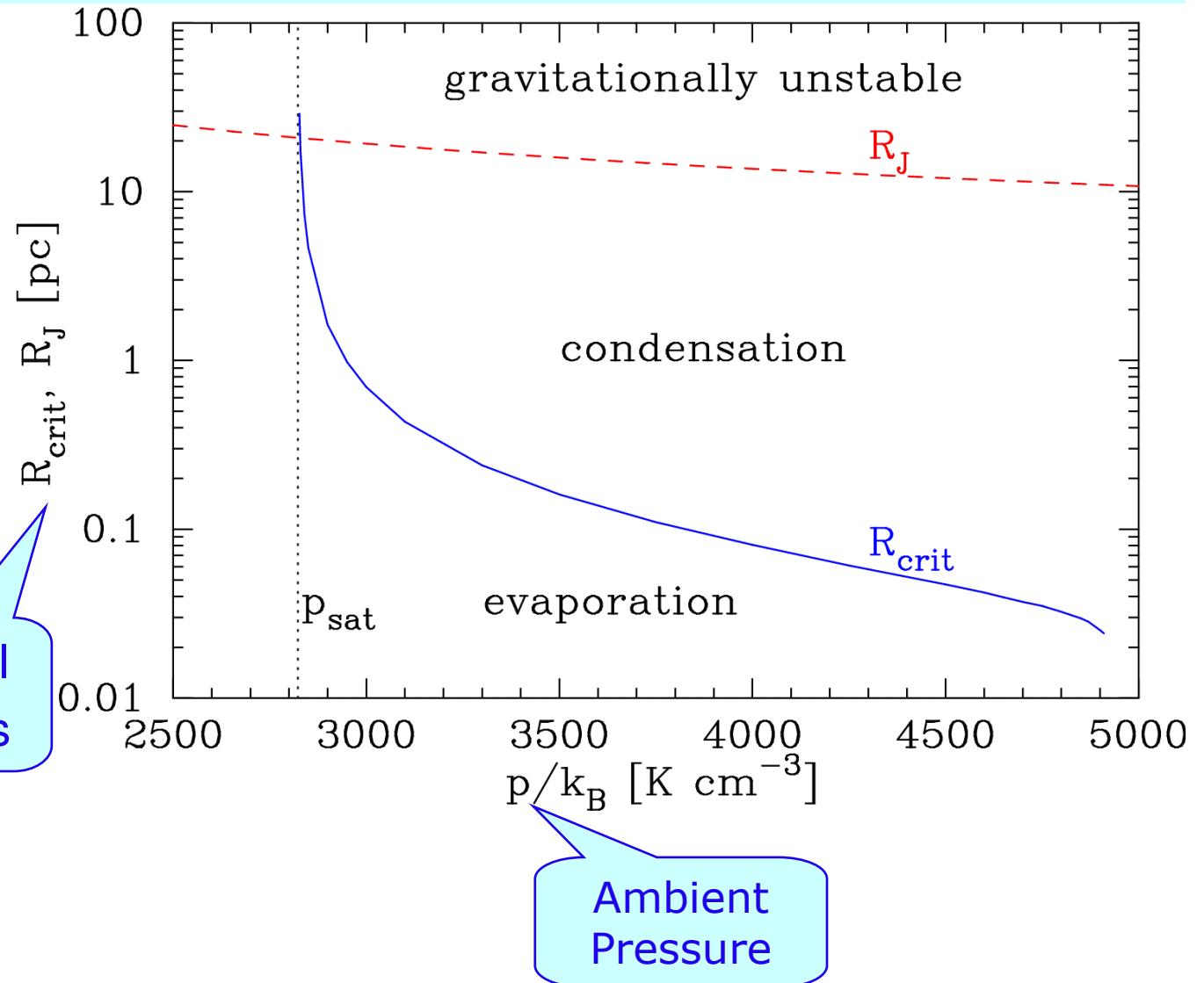


pressure is larger,  
the critical size of  
the stable cloud  
is smaller.

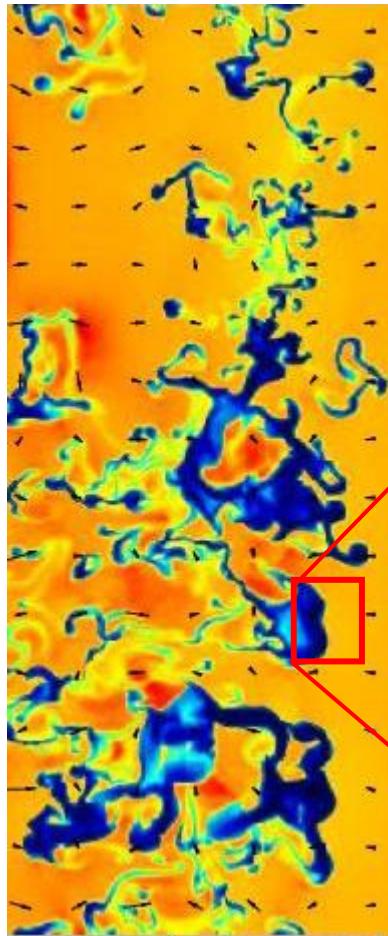
Critical  
Radius

"Tiny Scale  
Atomic  
Structure"?

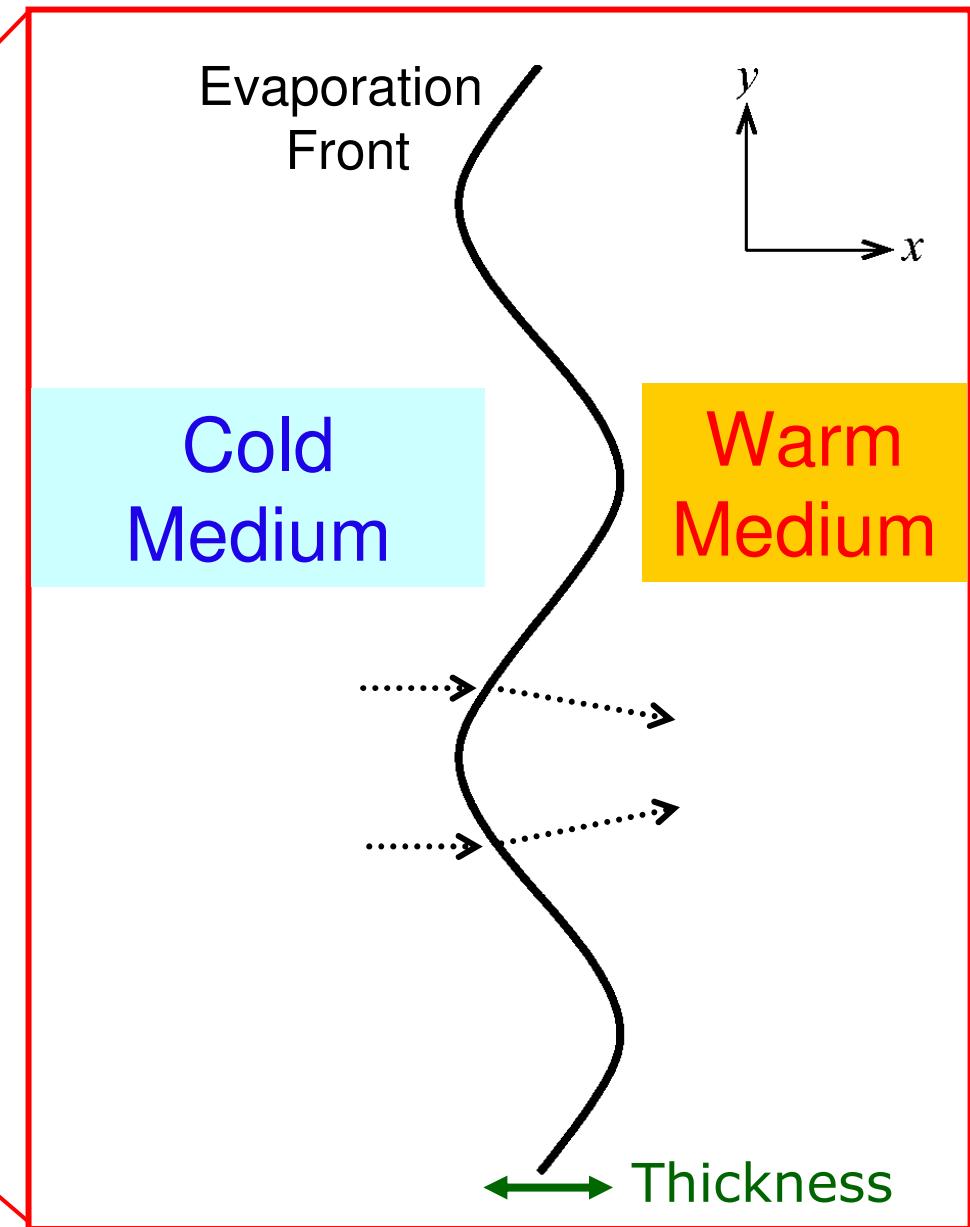
Braun & Kanekar 2005



# Instability of Transition Layer



important in maintaining  
the “turbulence”



# Instability of Transition Layer

Similar Mechanisms...

## 1) Darrieus-Landau (DL) Instability

Flame-Front Instability

# Important in SNe Ia

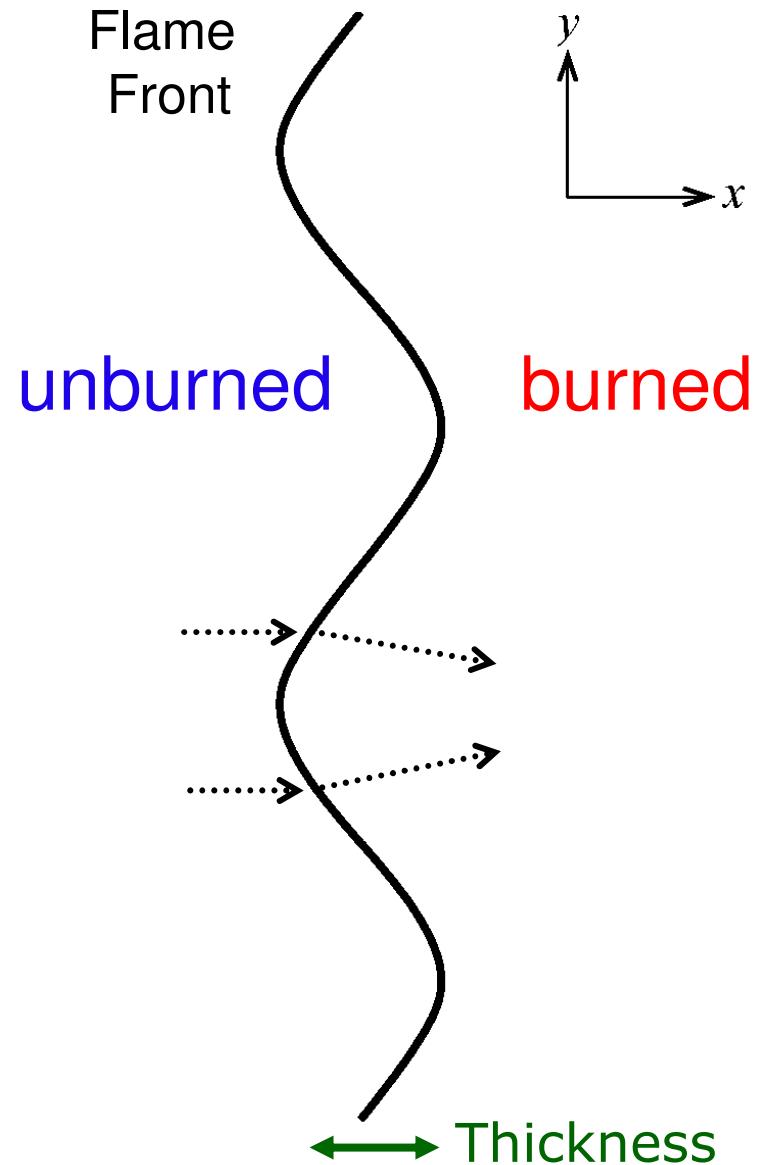
# Effect of Magnetic Field

See Dursi (2004)

## 2) Corrugation Instability in MHD Slow Shock

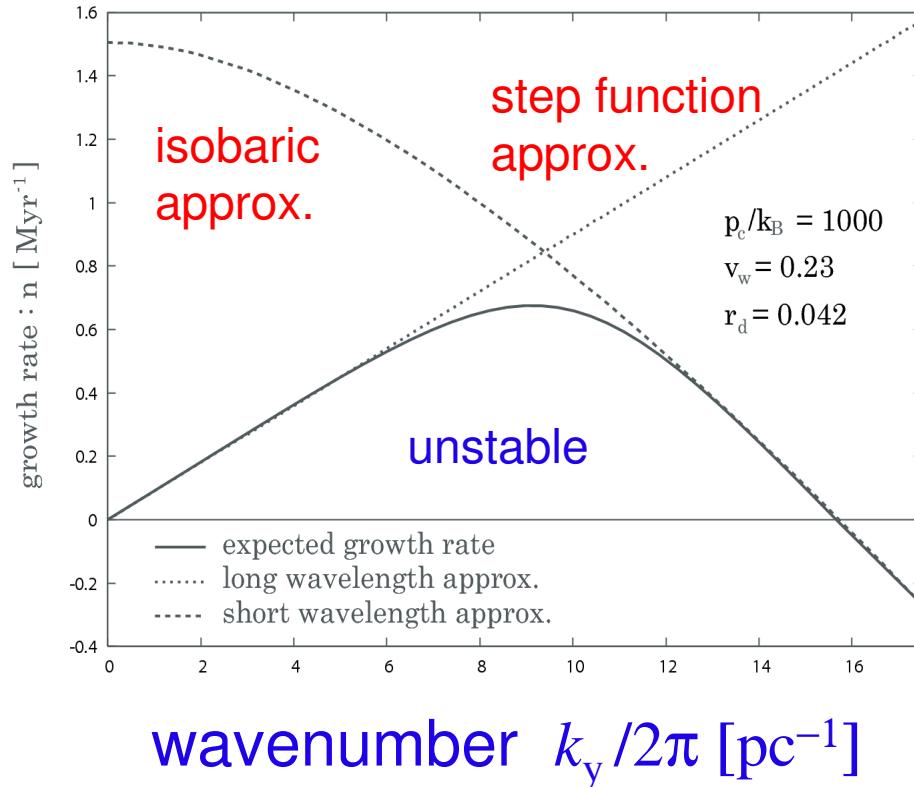
– Edelman 1990

– Stone & Edelman 1995

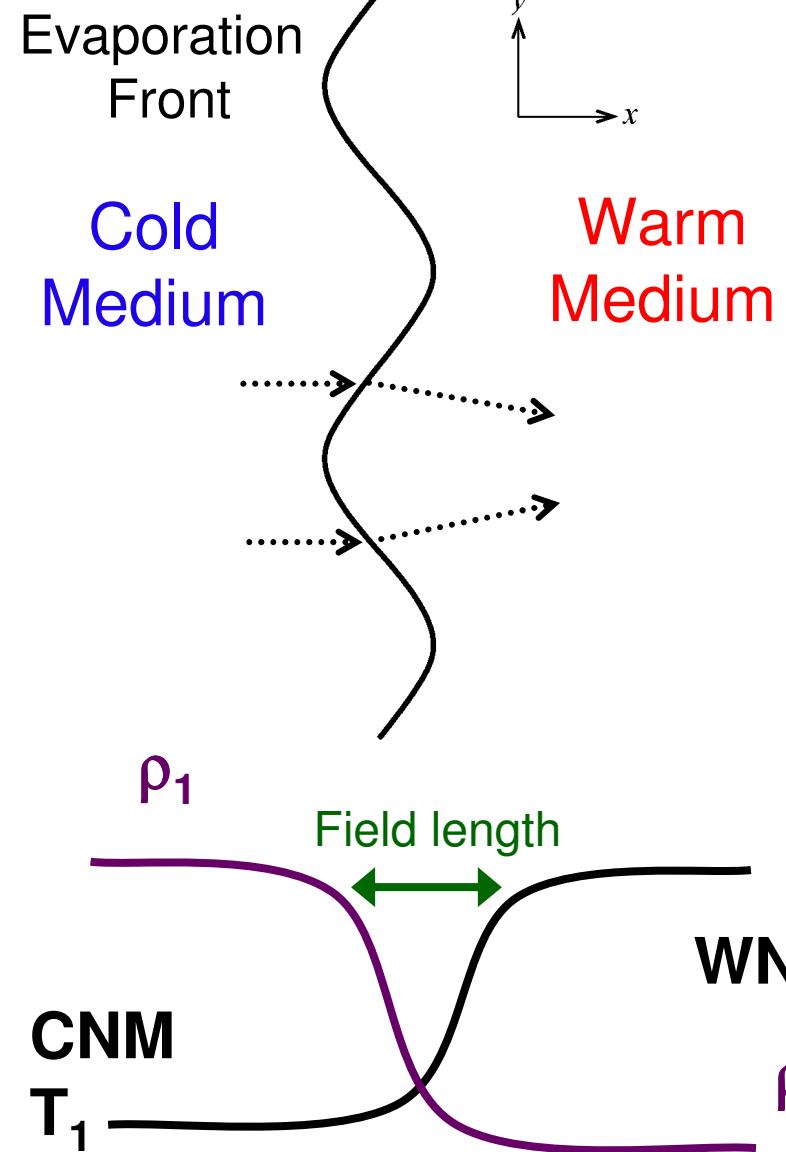


# Linear Analysis of New Instability

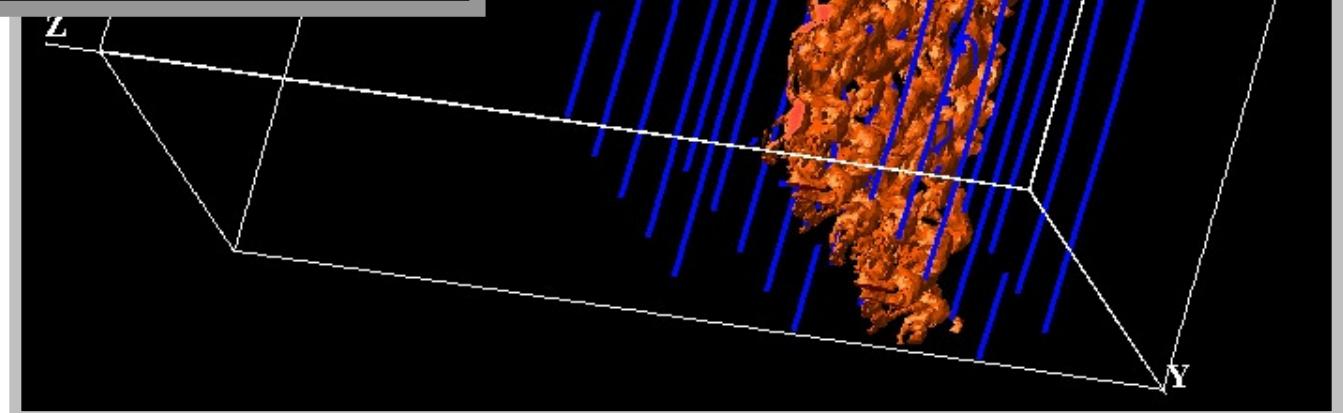
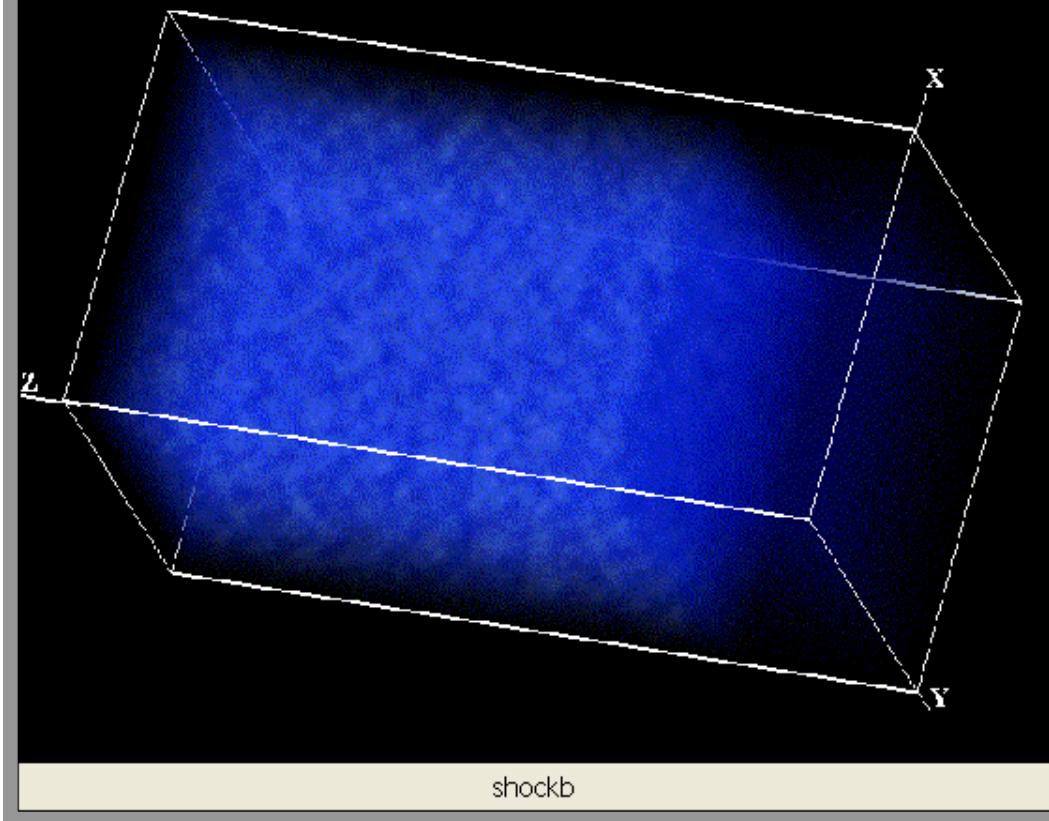
## Growth Rate ( $\text{Myr}^{-1}$ )



Inoue, Inutsuka, & Koyama  
2006, ApJ 652, 1131



WNM Swept-Up by MHD Shock (3D)  
Koyama & Inutsuka 2002



WNM Swept-  
Up by MHD  
Shock (3D)

# Effect of Magnetic Field on TI

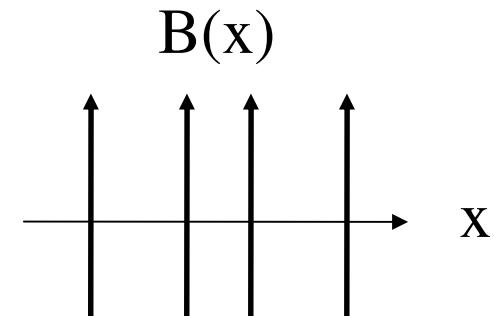
TI growth until gas reaches stable phase.

But, Magnetic field can prevent TI.

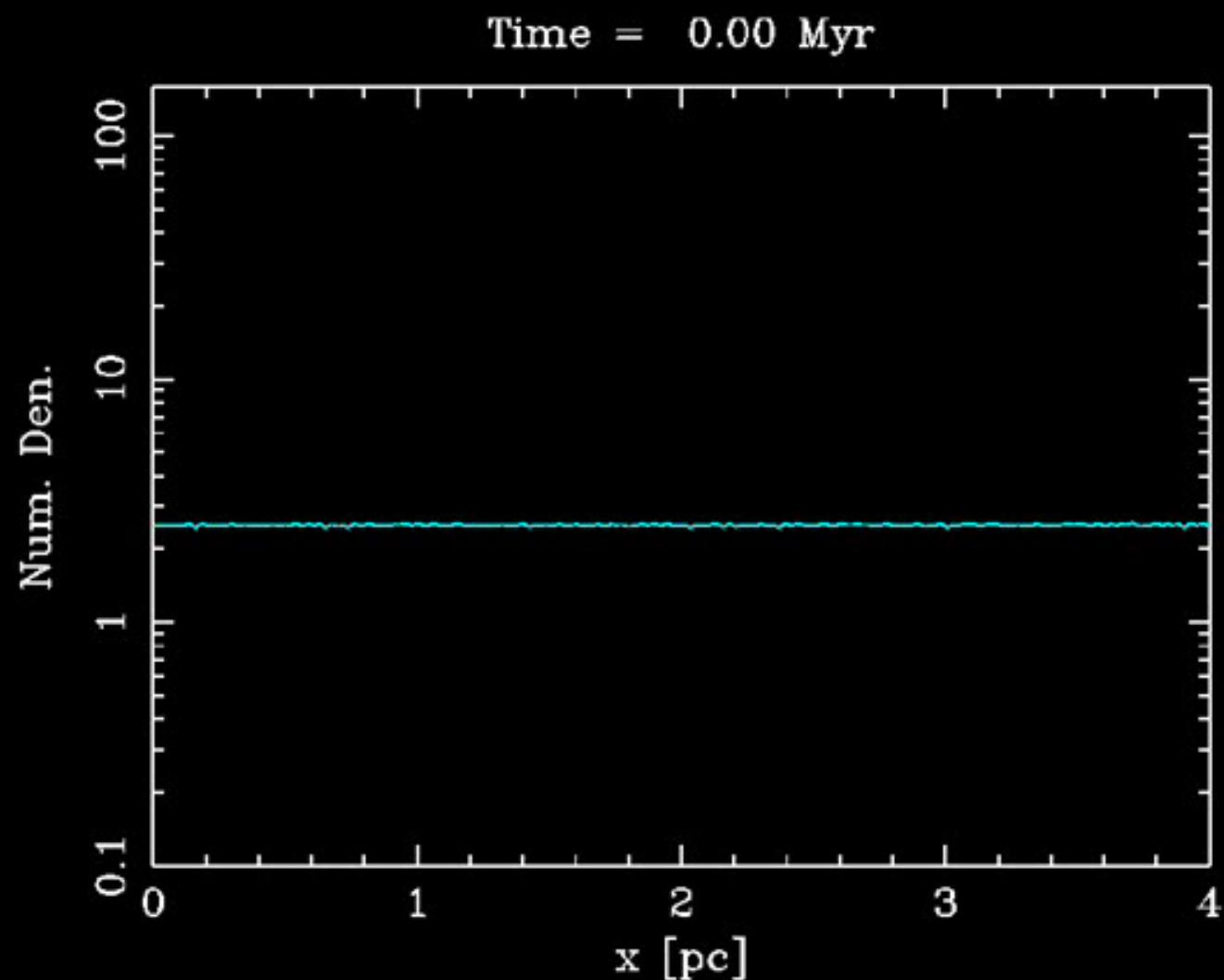
Actually, ISM is a partially ionized medium.

Can ambipolar diffusion reduce magnetic field in CNM?

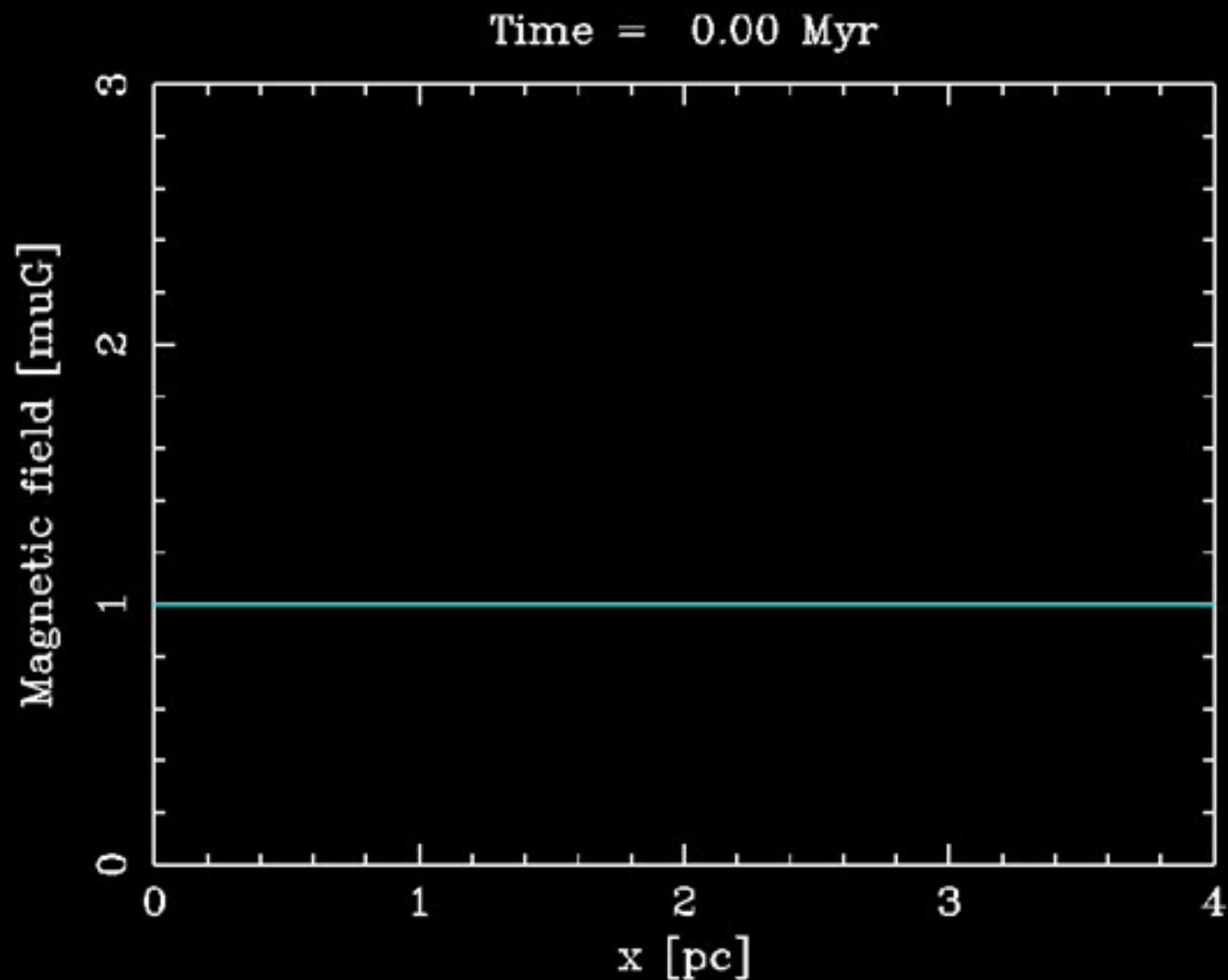
We perform 1D simulations of TI with transverse MF & Ambipolar diffusion.



# Model 2 : $B_{\text{ini}}=1 \mu \text{ G}$

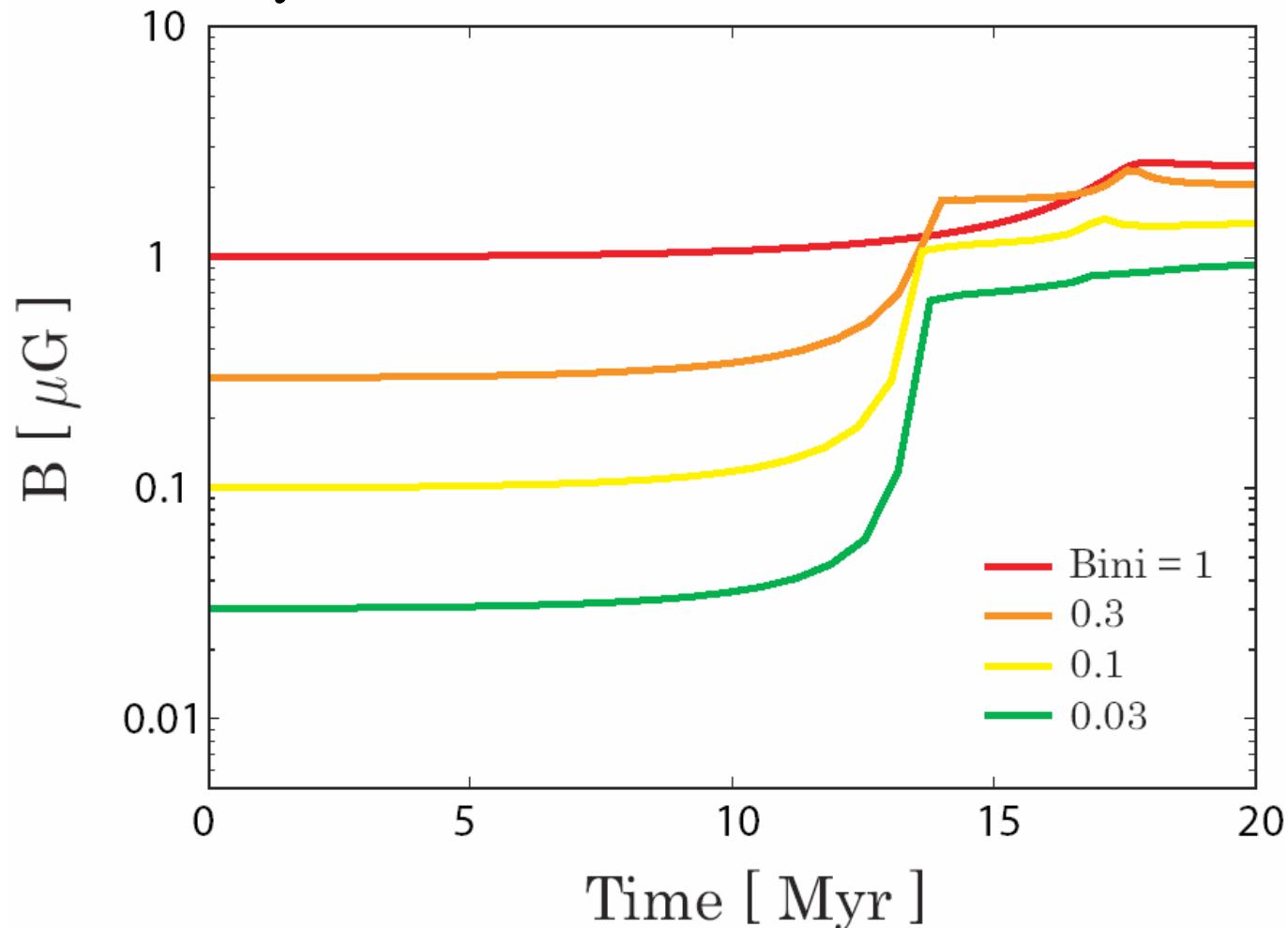


# Model 2 : $B_{\text{ini}}=1 \mu \text{G}$



# Evolution of Magnetic Intensity

Magnetic intensity growth to a few  $\mu\text{G}$  irrespective of initial intensity!



Inoue, Inutsuka, & Koyama (2006) ApJ **658**, L99

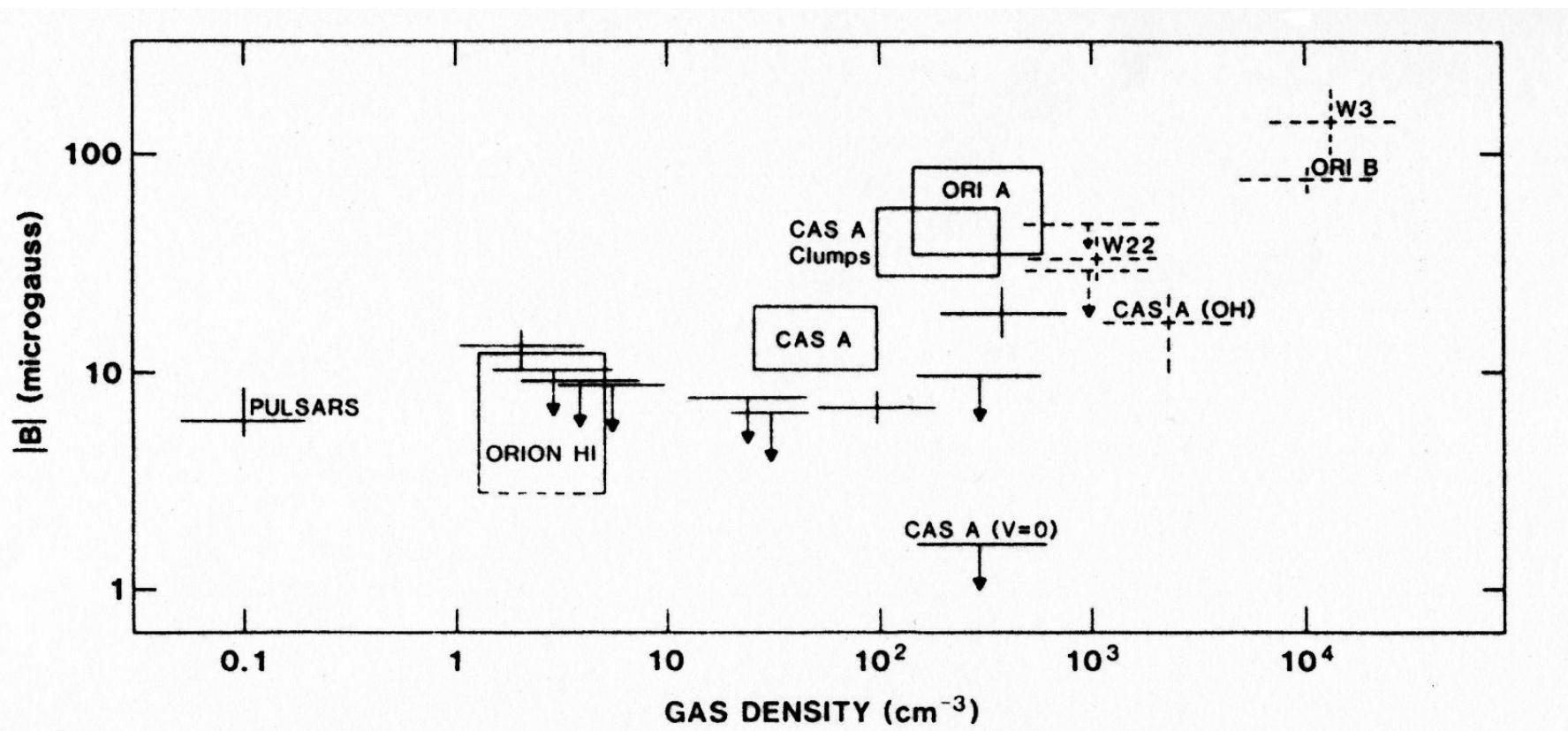
# Magnetic Intensity in CNM

- Condensation speed of TI:  $v_{\text{TI}} = \lambda_F / t_{\text{cool}}$
- If  $v_{\text{TI}} < v_{\text{drift}}$ , magnetic field lines do not accumulate. → TI is easy.
- If  $v_{\text{TI}} > v_{\text{drift}}$ , magnetic field lines accumulate.
- $V_{\text{TI}} \approx V_{\text{drift}}$  determine critical Magnetic intensity  $B_{\text{AD}}$ :

$$B_{\text{AD}} \simeq 3.2 \left( \frac{p_n/k_B}{4000 \text{ K cm}^{-3}} \right)^{1.475} \left( \frac{n_n}{50 \text{ cm}^{-3}} \right)^{-0.4875} \mu\text{G}$$

Inoue, Inutsuka, & Koyama (2006) ApJ **658**, L99

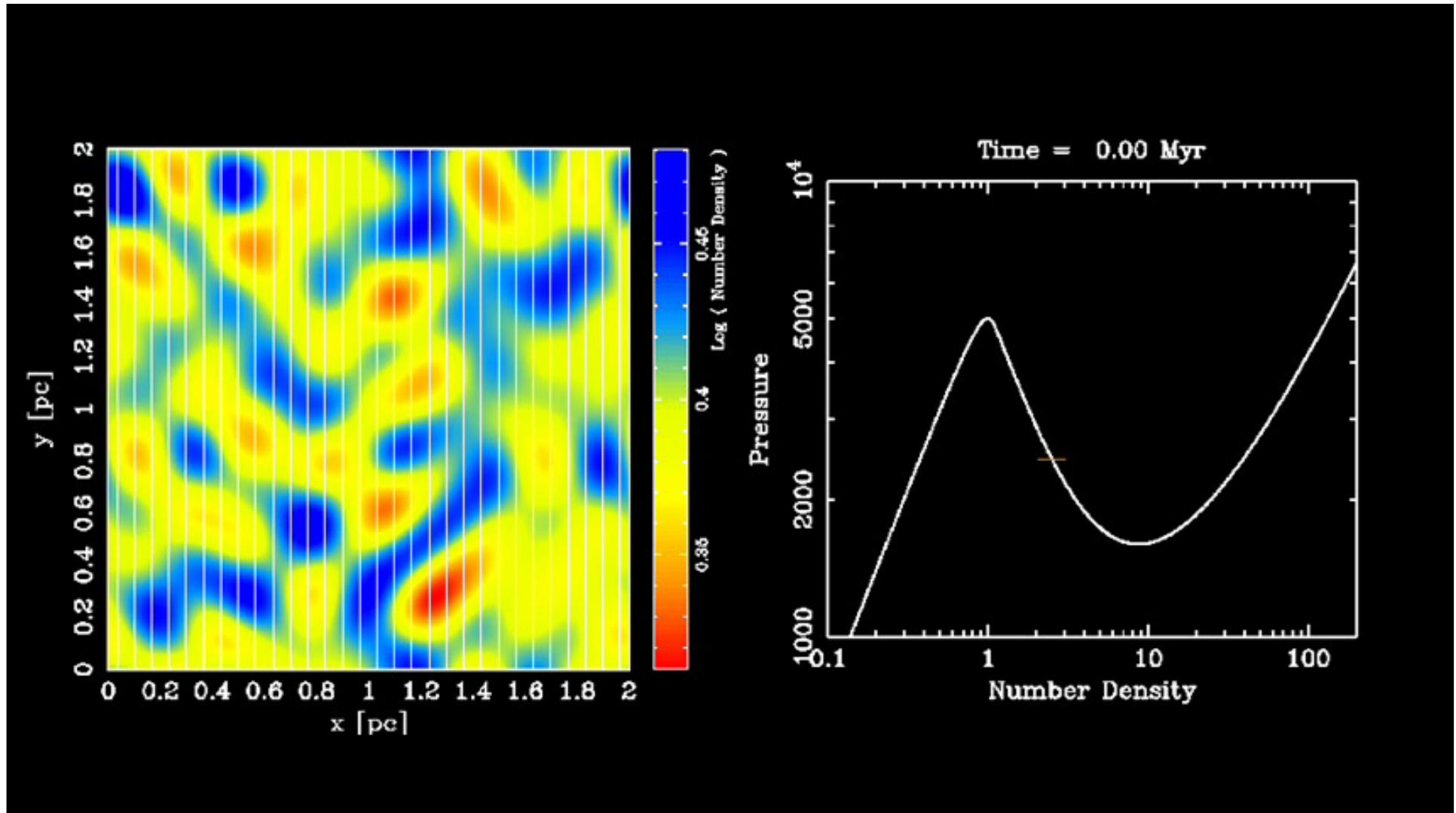
# Observed Magnetic Field Intensity vs. Density



Troland & Heiles 1986

# 2D 2-Fluid MHD Simulations

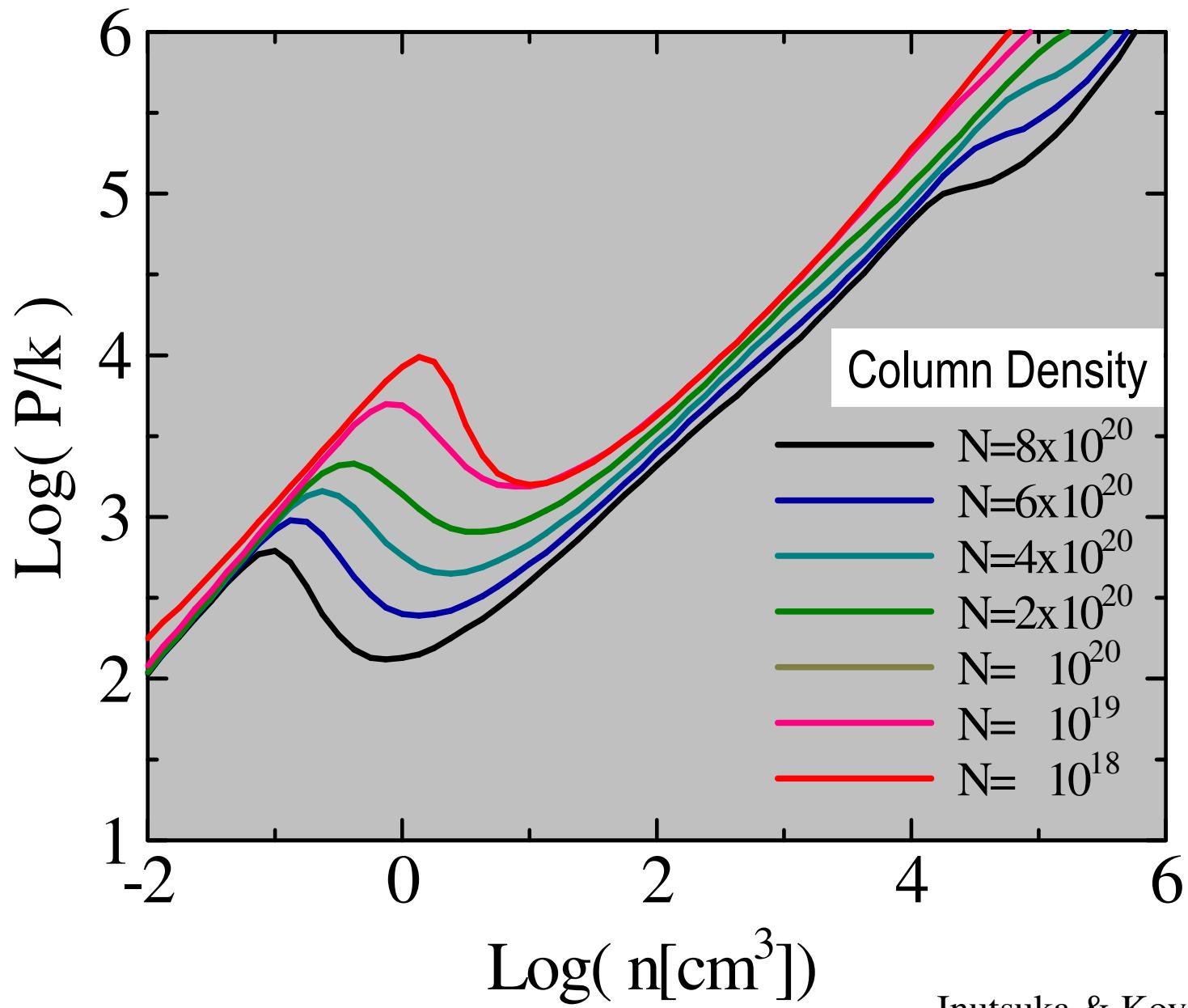
Preliminary!



# Further Evolution into Molecular Clouds?

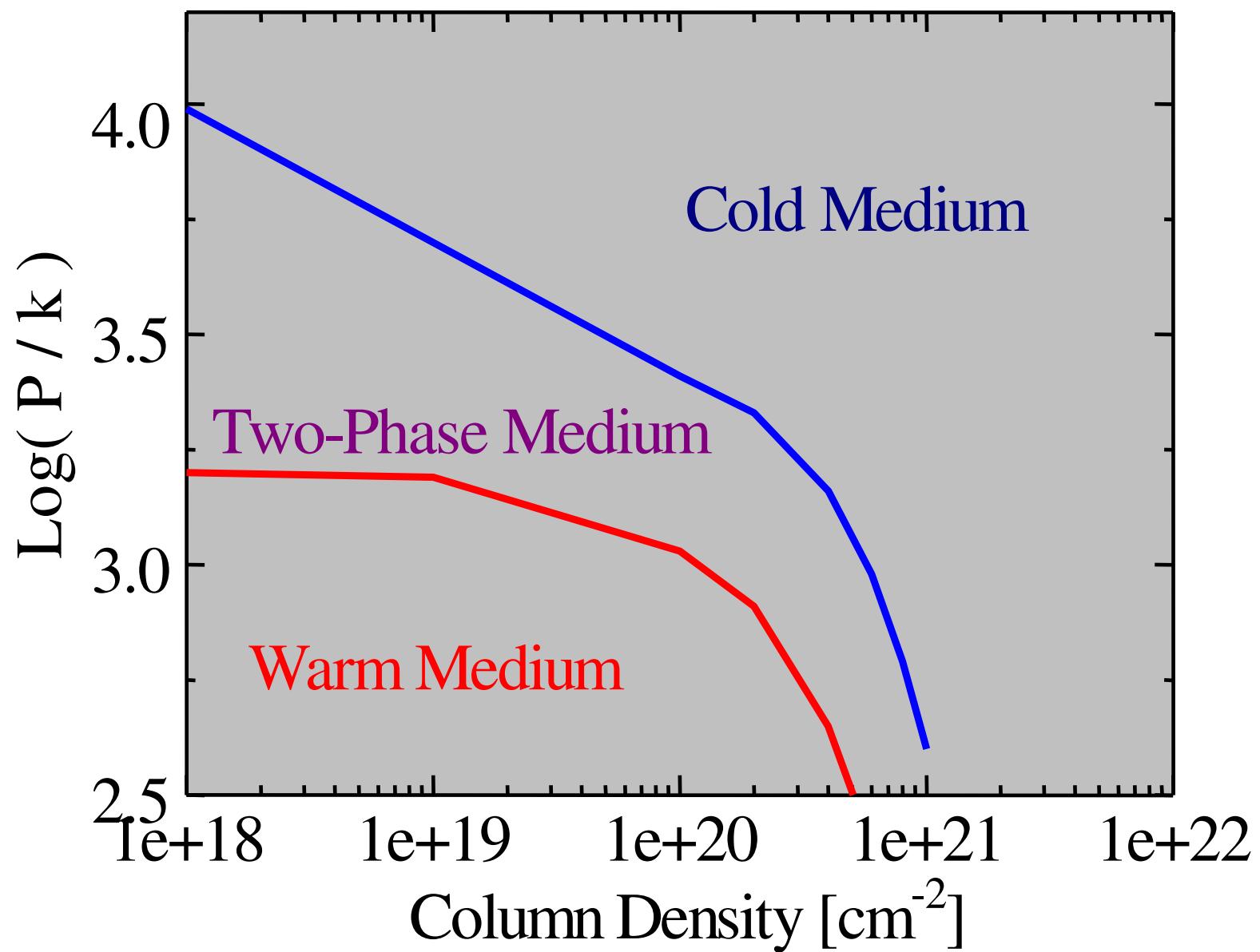
- Higher Column Density?
- Higher Density?

# Equilibrium with Various Column Density



Inutsuka & Koyama 1999

# Allowed Region of 2-Phase Medium



Inutsuka & Koyama 1999

When column density is sufficiently large,

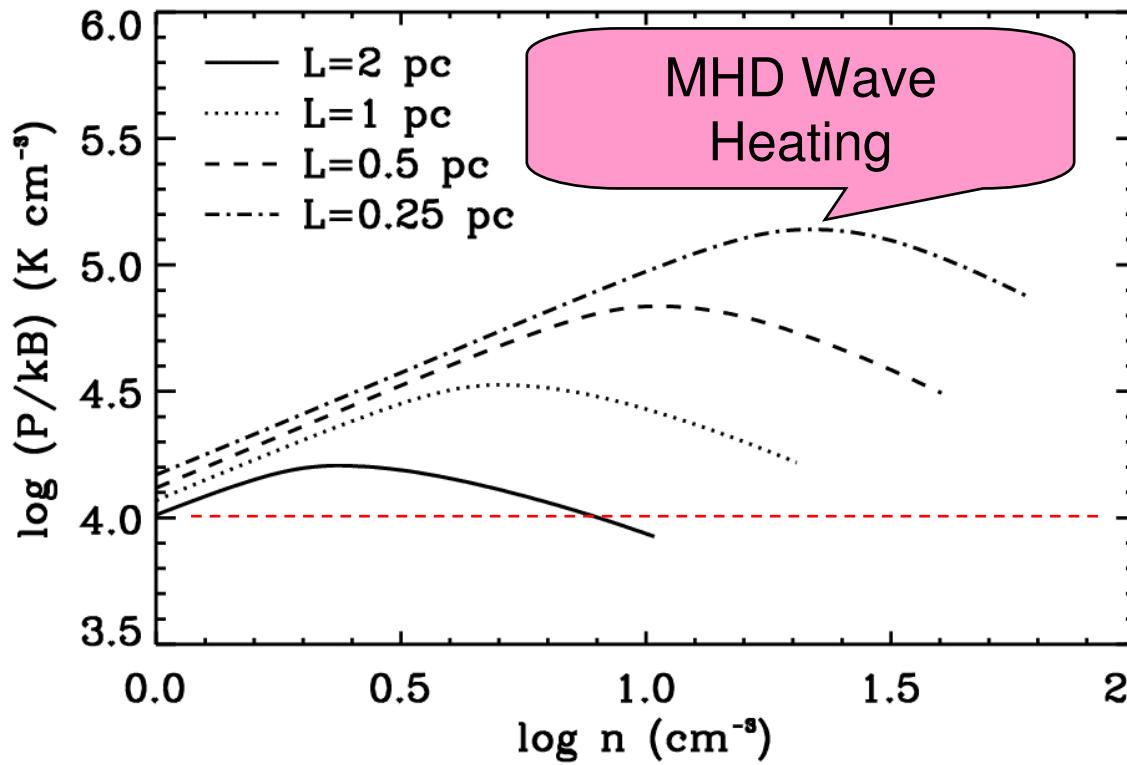
$$N_H > 10^{21} \text{ cm}^{-2} \text{ or } A_v > 1 \text{ mag}$$

ambient radiation field does not provide sufficient radiative heating for WNM.

Without any heating WNM simply cools down very quickly.

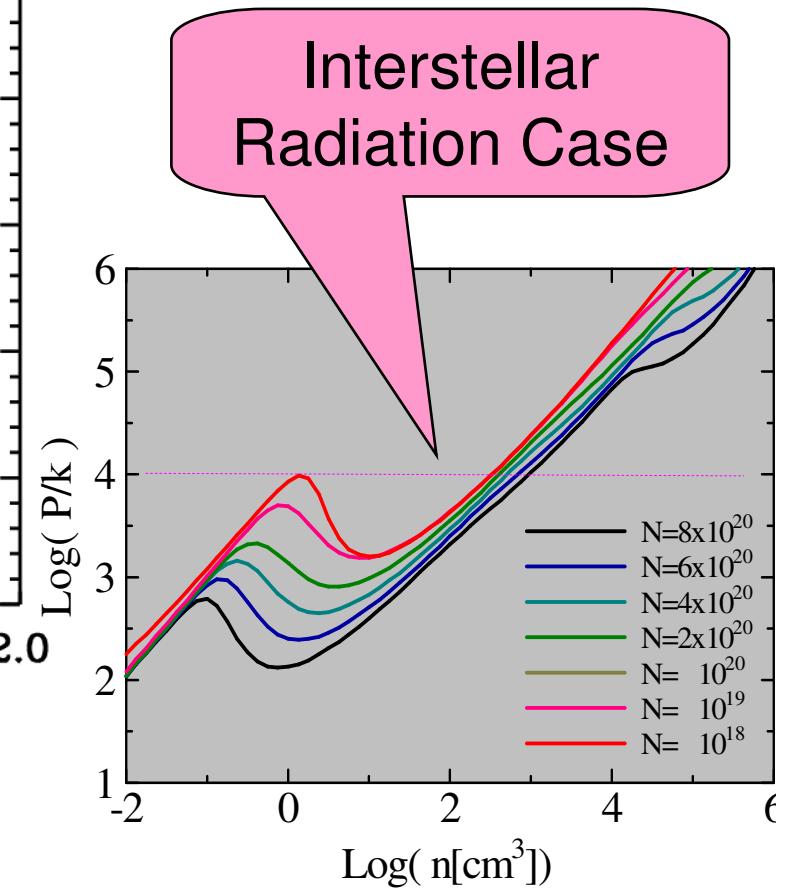
Is there any heating to WNM  
inside Molecular Clouds?

# WNM in Molecular Clouds: Thermal Equilibrium with MHD Wave Heating



$$P_{\text{MC}} = nT = 10^4(n/10^3)(T/10\text{K})$$

Heating is **sufficient** for WNM to **survive** in MC.



Hennebelle & Inutsuka 2006  
ApJ 647, 404

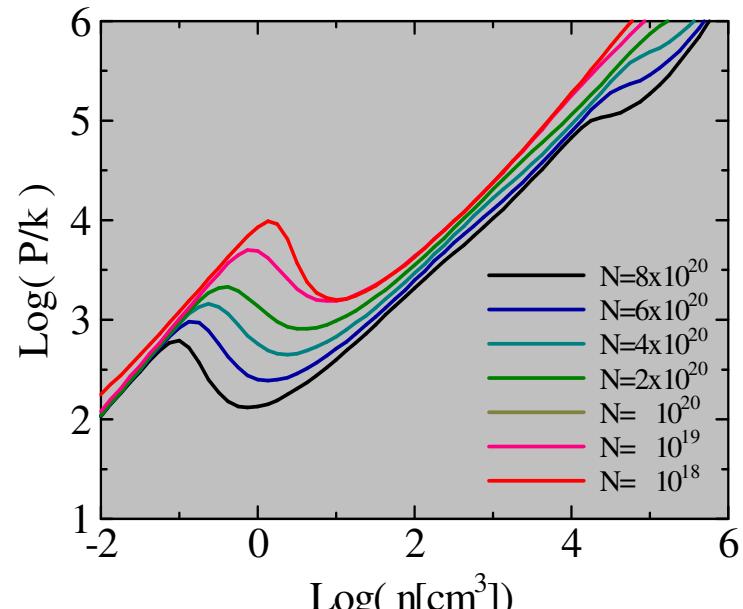
# Summary

- Shock waves in ISM create turbulent CNM embedded in WNM.
- In TI-driven turbulence in Multi-Phase ISM
  - Evaporation/Condensation of CNM clouds
  - New Instability in Evaporation Front
- Can WNM Survive in Molecular Clouds?
  - Possible: Dissipation of MHD Waves

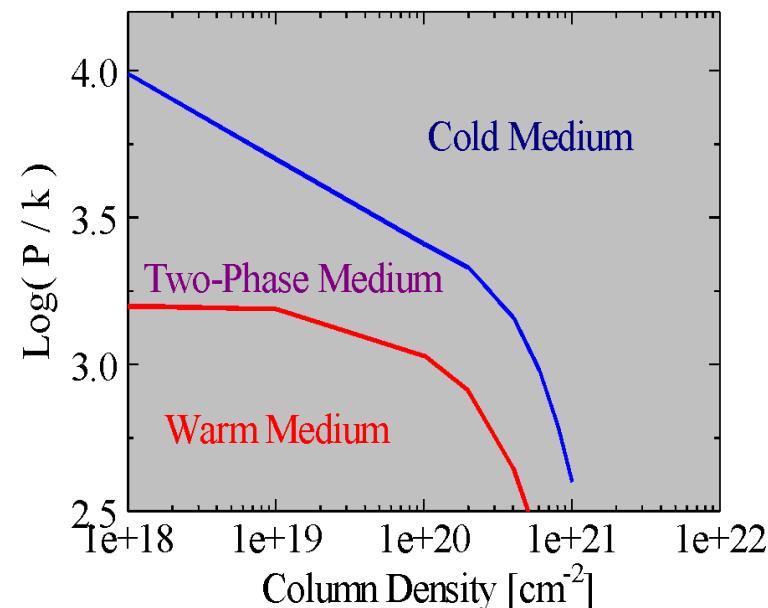
## Future Work

- RHD calculation of the evolution of two phase medium...
- When self-gravity becomes important?

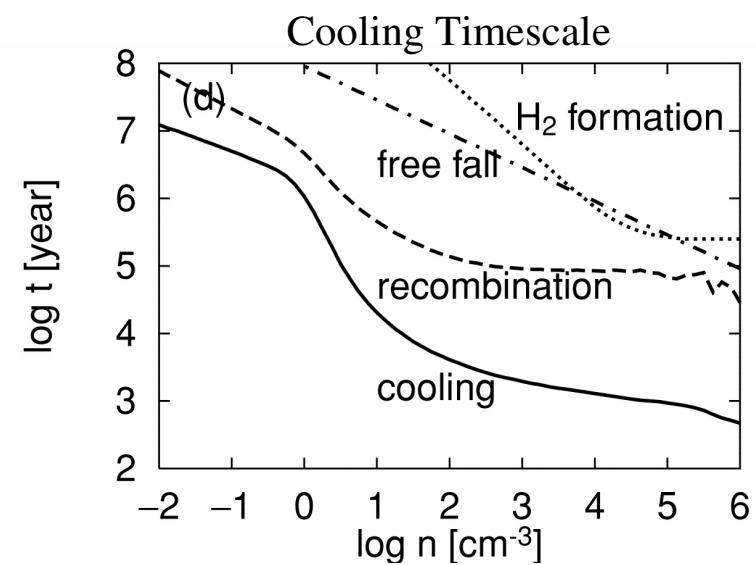
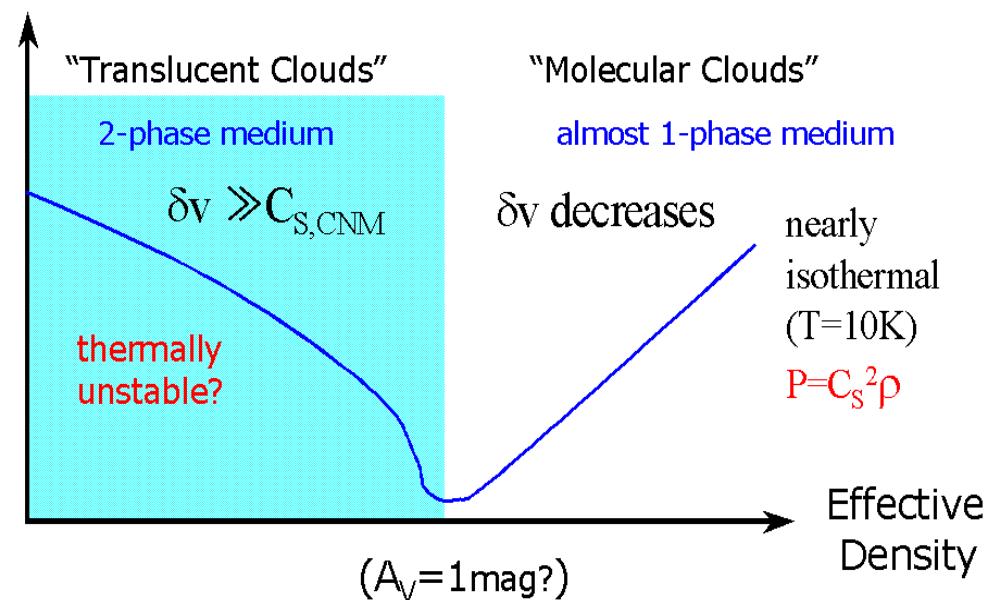
# Radiative Equilibrium: Column Density Dependence



Effective Pressure



Inutsuka & Koyama 2000



# Dynamical Timescale of ISM

## Dynamical Three Phase Medium

- McKee & Ostriker 1977
- SN Explosion Rate in Galaxy...  $1/(100\text{yr})$
- Expansion Time...  $1\text{Myr}$
- Expansion Radius...  $100\text{pc}$

$$(10^{-2} \text{ yr}^{-1}) \times (10^6 \text{ yr}) \times (100\text{pc})^3 = 10^{10} \text{ pc}^3 \sim V_{\text{Gal.Disk}}$$

$(10\text{kpc})^2 \times 100\text{pc}$

Dynamical Timescale of ISM  $\sim 1\text{Myr}$

« Timescale of Galactic Density Wave  $\sim 100\text{Myr}$